

# Quantifying Instruction Criticality for Shared Memory Multiprocessors

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# Overview

- All instructions are NOT created equal
  - With respect to impact on performance → criticality
- Example (a 2-processor shared memory system):

*processor 1*

$r3 = r1 + r2$

**store r3, 0x1000**

$r3 = r3 * r5$

$r4++$

*data  
dependence*



*processor 2*

$g1 = g2 / g3$

$g4++$

**load g5, 0x1000**

$g2 = g4 + g5$

- Contributions of this work
  - Create model for determining criticality in MP systems
  - Devise algorithm for computing criticality
  - Evaluate criticality of real MP workloads
- But why do we care about criticality?

# Multiprocessor Control Policies

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If the system knew instruction criticality dynamically, how could this be helpful?

- **Power efficiency**
  - Less critical instructions can run more slowly
- **Resource utilization**
  - Critical-instruction-first resource allocations
- **Misspeculation reduction**
  - Turn off speculation for less critical instructions

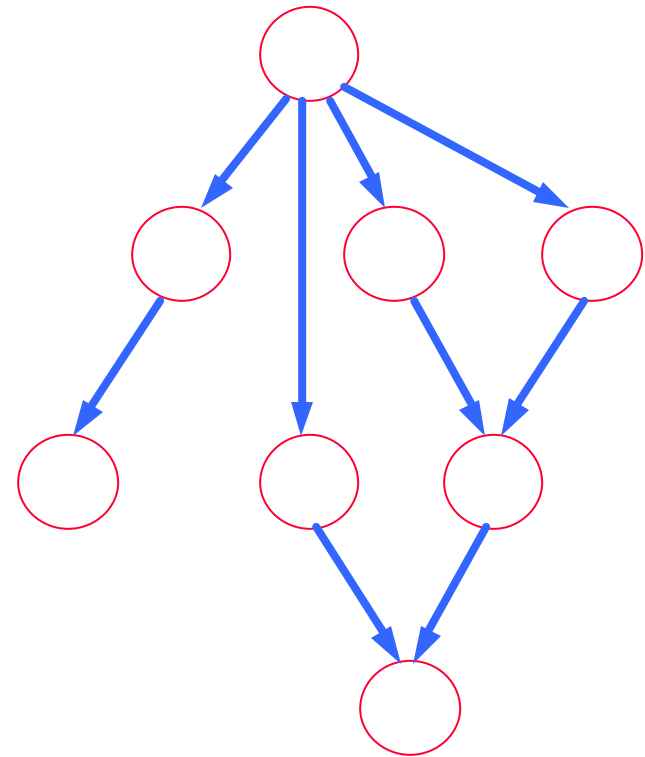
# Outline

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- Motivation
- A directed acyclic graph (DAG) model for execution
  - Critical path and slack
  - Mapping DAGs to multiprocessor systems
  - Computing slack
- Graph Reduction
- Evaluation
- Related work
- Conclusions and future work

# A DAG Model for Program Execution

- **Node**: dynamic event during execution (e.g., fetching an instruction, executing a task)
- **Edge**: dependence between source and sink nodes (e.g., data dependence)
  - **Weighted** by the time to resolve the dependence
- **Critical path**: longest weighted path in the DAG  
(CP length = runtime)



We study *spectrum of criticality*, not just on or not on the critical path

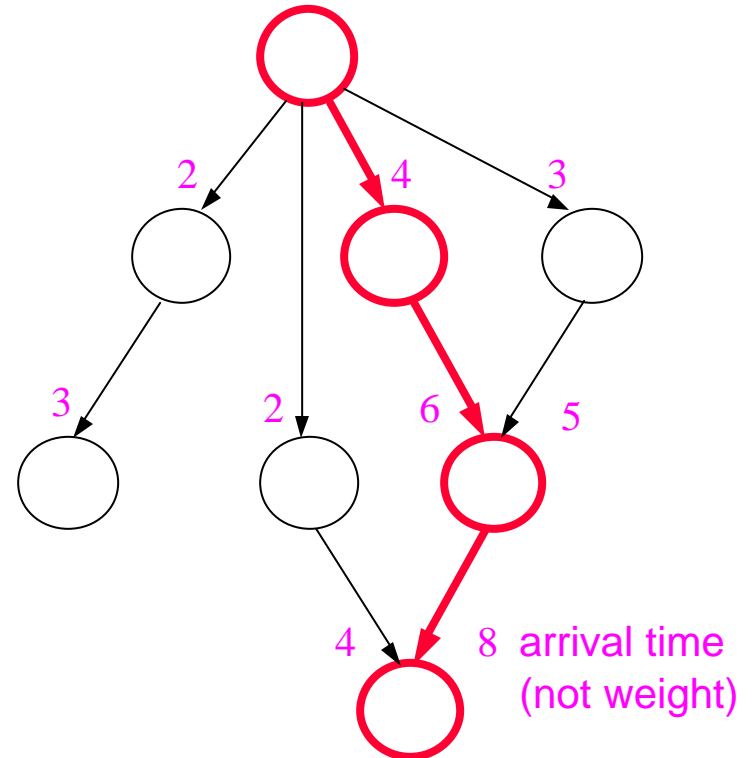
# Criticality

- **Criticality**: importance level of event to overall performance

**Fields et al. (ISCA '02):**

- **Global slack**: how long the start time of an event (node) can be delayed without affecting program runtime (criticality!)
- **Edge arrival time**: time *at which* the represented dependence is resolved during execution
- **Last arriving edge**: edge that arrives last at the sink node

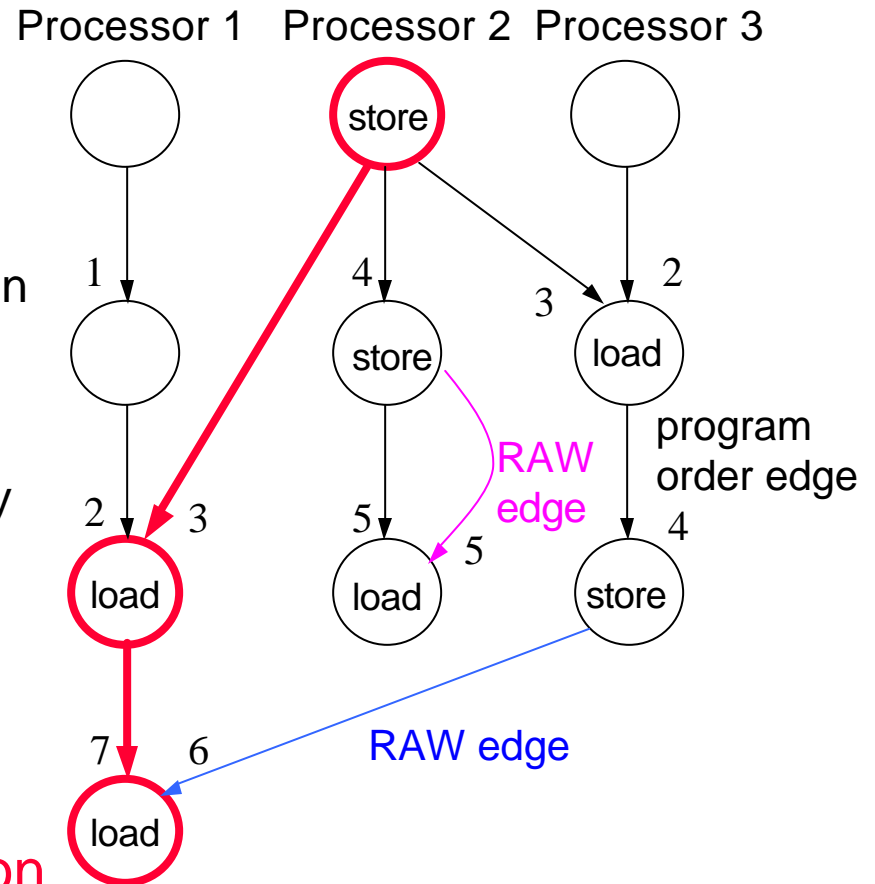
Previous work applies criticality to uniprocessors.  
We extend it to multiprocessors



*An edge on a critical path must be a last-arriving edge; A non-last-arriving edge must not be on a critical path*

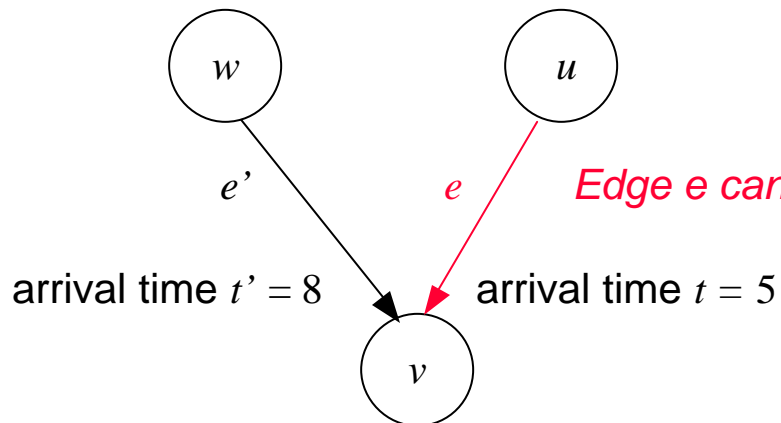
# Multiprocessor Criticality

- Extension of uniprocessor DAG model (Fields et al. ISCA'01, ISCA'02)
- In-order processors
  - Each node represents an instruction
- Shared memory system
  - Processors communicate only via loads and stores to shared memory
- Two types of dependence (edges)
  - *Program order*
  - *Read-after-write (RAW)*
- **Global slack quantifies instruction criticality, but how to compute it?**



# Local Slack: A Tool for Global Slack

- The *local slack* of an edge  $e = (u, v)$ , denoted by  $L(e)$ , is the time that the latency of  $e$  can be increased without delaying its sink node  $v$ . (Fields et al. ISCA 2002)
- Properties
  - If an edge is not last-arriving, then it can be delayed
  - If an edge is last-arriving, then it cannot be delayed



*Edge  $e$  can be delayed for 3 time units*

$$L(e) = \max(t, t') - t$$

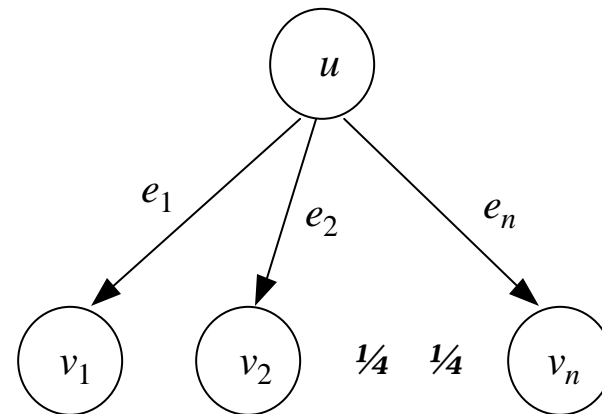
$$L(e') = \max(t, t') - t'$$

Based on local slack, we can compute global slack



# Computing Global Slack

- The *global slack* of a node  $u$ , denoted by  $G(u)$ , is the maximum time  $u$  can be delayed without extending the critical path of the DAG (Fields et al. ISCA 2002)
- An instruction's global slack quantifies its criticality
- A node's global slack depends on local slack of its outgoing edges and global slack of its children
- To compute global slack for all nodes, we need to process the **entire DAG**



$$G(u) = \min_i (L(e_i) + G(v_i))$$

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- **Graph Reduction**
- Evaluation
- Related work
- Conclusions and future work

# Graph Reduction

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- We compute global slack offline, but processing DAGs requires large amounts of storage and time
  - Programs have billions of instructions
- We propose graph reduction to reduce DAGs
- Graph reduction dynamically removes DAG nodes and edges that **don't change the critical path and global slack of all nodes**
- Three theorems describe when a reduction can be performed dynamically during a program's execution
  - Details of theorems and proofs are in the paper

# Graph Reduction – Theorem 1

Program situation: Many instructions are neither loads nor stores. We can remove all of them!

*If*

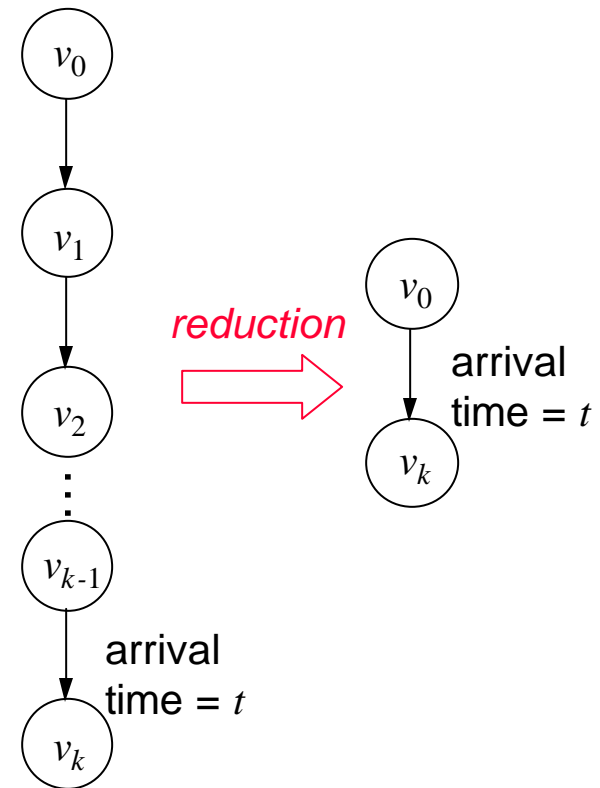
- $v_0, \dots, v_k$  are on the same processor
- $v_1, \dots, v_{k-1}$  are neither loads nor stores

*Then*

- The DAG can be reduced by removing  $v_1, \dots, v_{k-1}$  and retaining arrival time  $t$

*Why?*

- $G(v_1) = G(v_2) = \dots = G(v_{k-1}) = G(v_k)$
- If  $v_1, \dots, v_{k-1}$  are on the critical path, then  $v_0$  and  $v_k$  must be on the critical path of the reduced DAG



# Graph Reduction – Theorem 2

Program situation: A sequence of loads on the same processor read the same value written by a store. We could remove all these RAW edges except the first one!

*If*

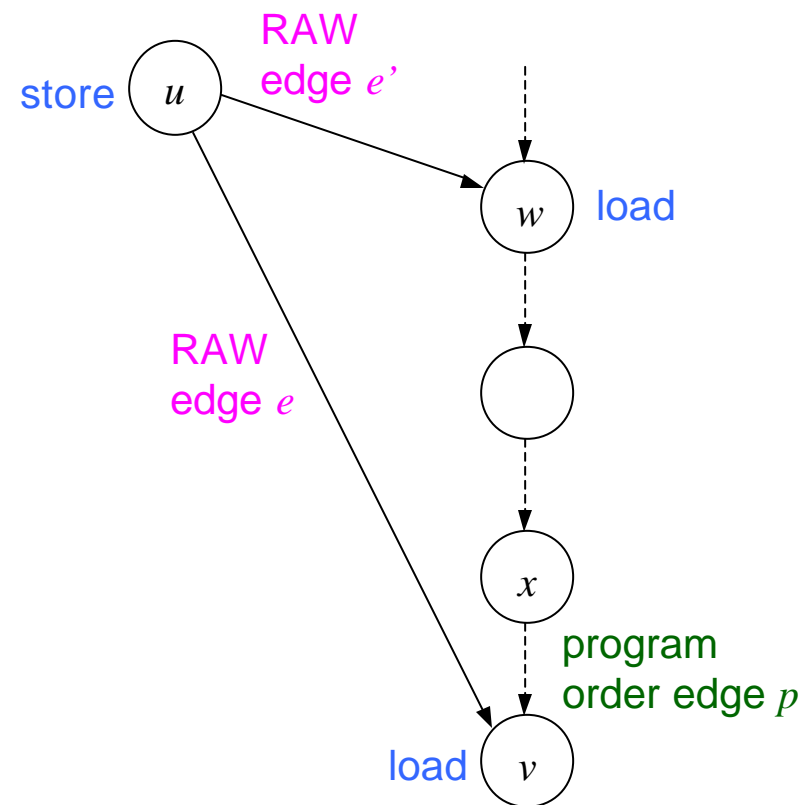
- Arrival time of  $e$  is less than arrival time of  $p$
- No node between  $w$  and  $v$  is the sink of a RAW edge that is last-arriving at the node

*Then*

- RAW edge  $e$  can be removed

*Why?*

- $e$  must not be on the critical path
- $e$  does not contribute to computing  $G(u)$  and  $G(x)$



# Graph Reduction – Theorem 3

Program situation: A load reads a value written by a store on the same processor. We could remove this RAW edge!

*If*

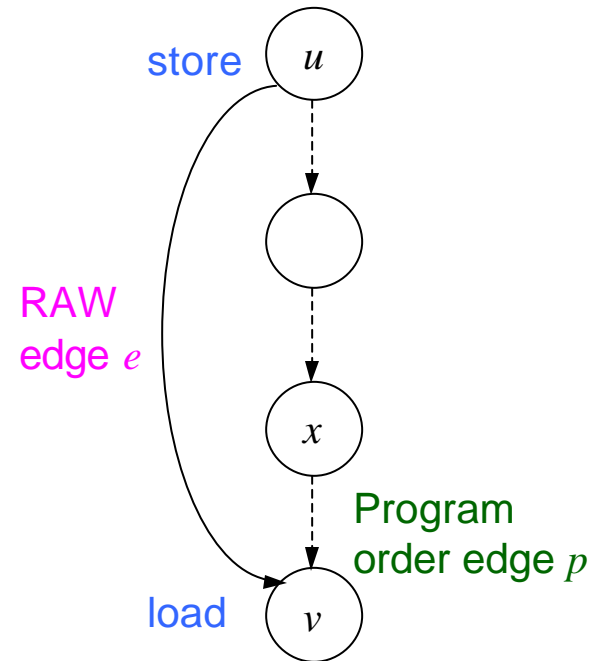
- Arrival time of  $e$  is less than arrival time of  $p$
- No node between  $u$  and  $v$  is the sink of a RAW edge that is last-arriving at the node

*Then*

- RAW edge  $e$  can be removed

*Why?*

- $e$  must not be on the critical path
- $e$  does not contribute to computing  $G(u)$  and  $G(x)$



# Outline

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- Motivation
- A directed acyclic graph (DAG) model for execution
- Graph Reduction
- **Evaluation**
  - Methodology
  - Results
- Related work
- Conclusions and future work

# Experiments

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- Do instructions really have global slack? How much?
- How critical is an entire processor in a program's execution?
- How do different cache coherence protocols affect global slack of instructions?
- How effective is graph reduction?



# Methodology – Simulator

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- Simics
  - Full-system multiprocessor simulator
  - Functional simulator, can boot unmodified Solaris 8
  - A detailed memory hierarchy timing module
- Processor model
  - In-order processor core
  - Blocking cache requests
- Memory model
  - MOSI broadcast snooping cache coherence protocol
  - Sequential consistency

# Methodology – Workloads

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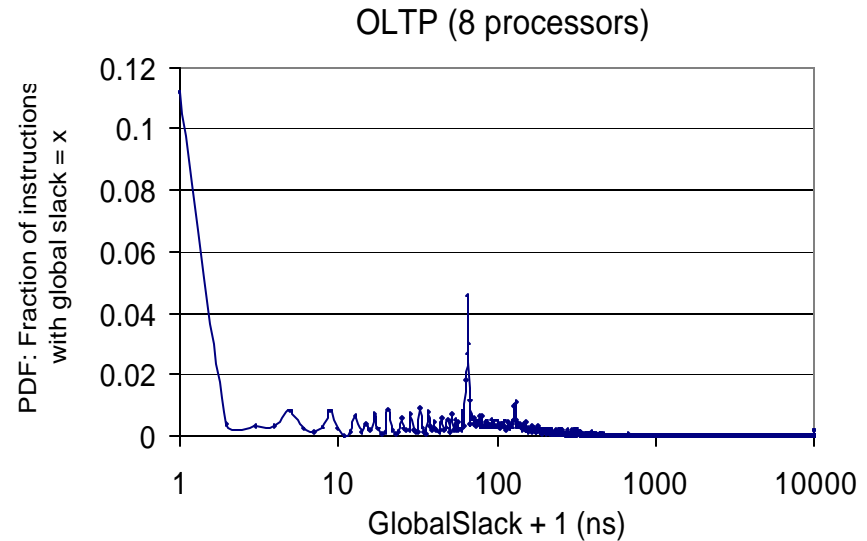
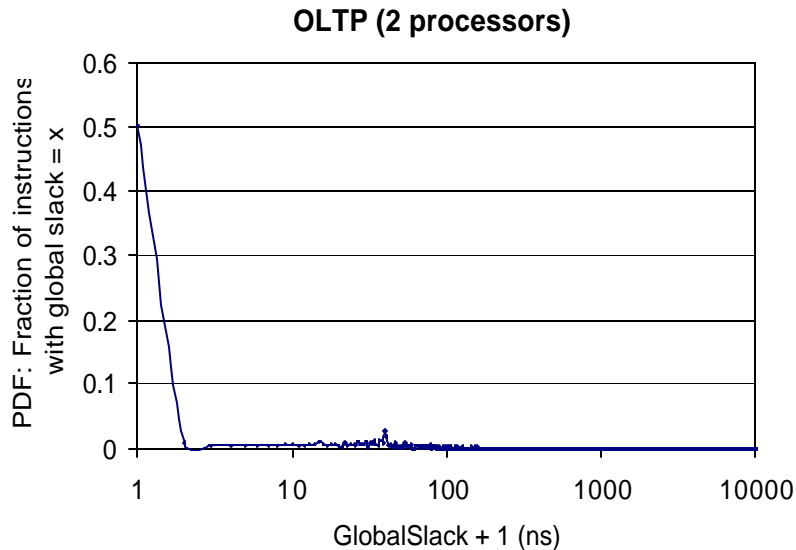
- Commercial workloads (Wisconsin suite)
  - *OLTP*: online transaction processing
  - *Java server*: SPECjbb2000 server-side java benchmark
  - *Static web server*: web server with static content
  - *Dynamic web server*: web server with dynamic content
- Scientific workloads (Stanford SPLASH-2)
  - *Barnes-Hut*: simulates the interactions of a system of bodies using the Barnes-Hut hierarchical N-body method
  - *Ocean*: simulates ocean movements using Gauss-Seidel multi-grid equation solver

# Methodology – Data Acquisition and Analysis

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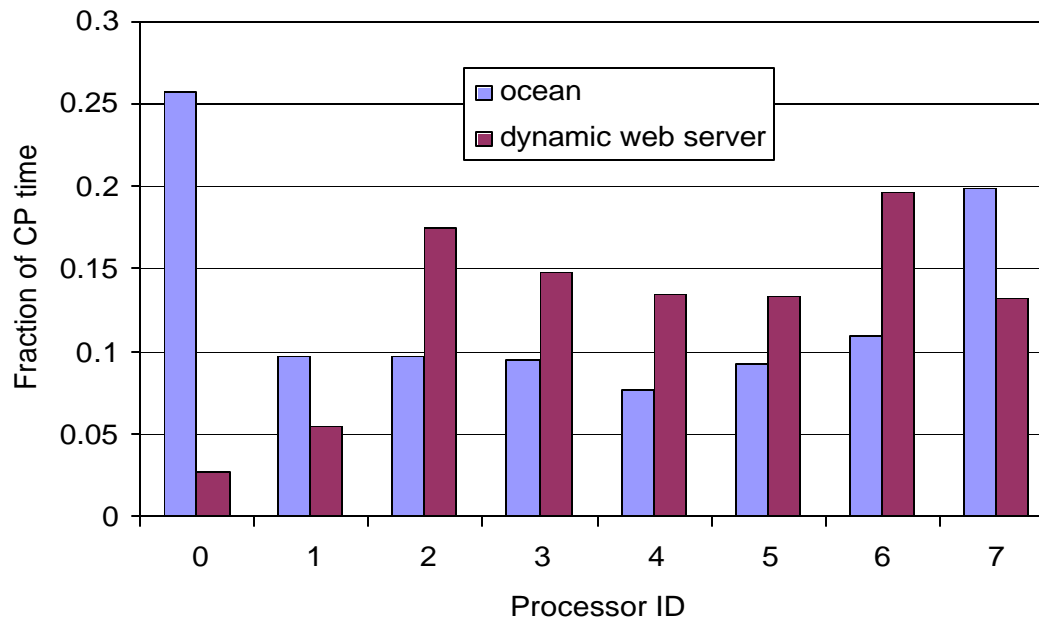
- Warm up simulated system for each workload
- Log dependences (edges) into files during execution
- Dynamically apply graph reduction during execution
- Construct DAG from log files
- Offline compute global slack for each instruction

# How Much Global Slack Exists?



- x-axis: global slack plus one in log scale
- y-axis: fraction of instructions that have global slack  $x$
- Most instructions have global slack  $< 100$  ns
- Spikes between 100 and 200 ns correspond to inter-processor communication latency
- Other workloads have similar results

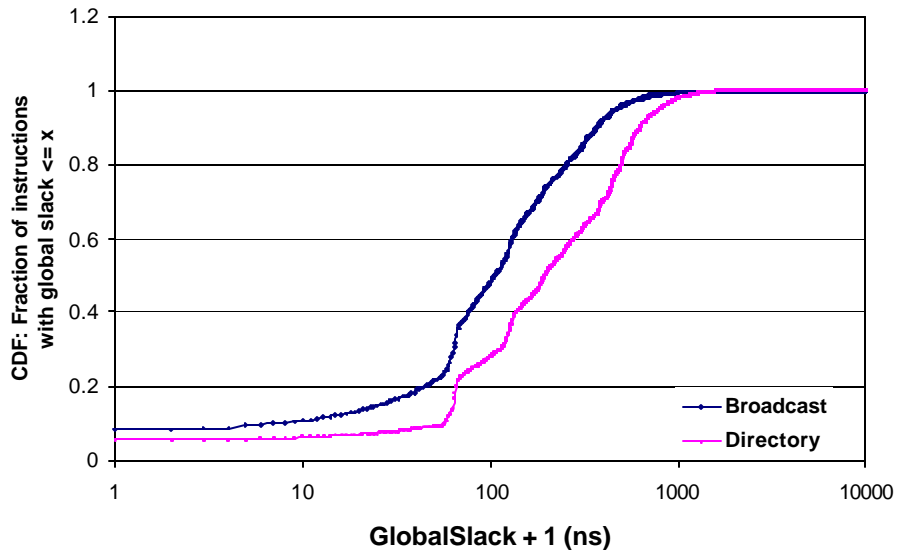
# Insight into Processor Criticality



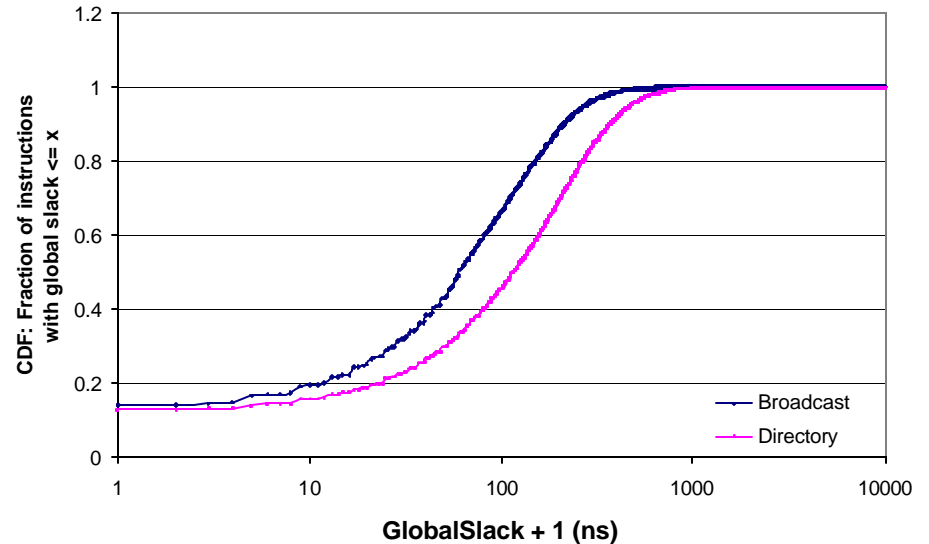
- x-axis: each processor in an 8-processor system
- y-axis: fraction of critical path's time spent on processor x
- Critical path time breakdowns closely correspond with processor L2 cache miss rates
- Other workloads have critical path evenly distributed

# Broadcast vs. Directory Protocols

## Static Web Server



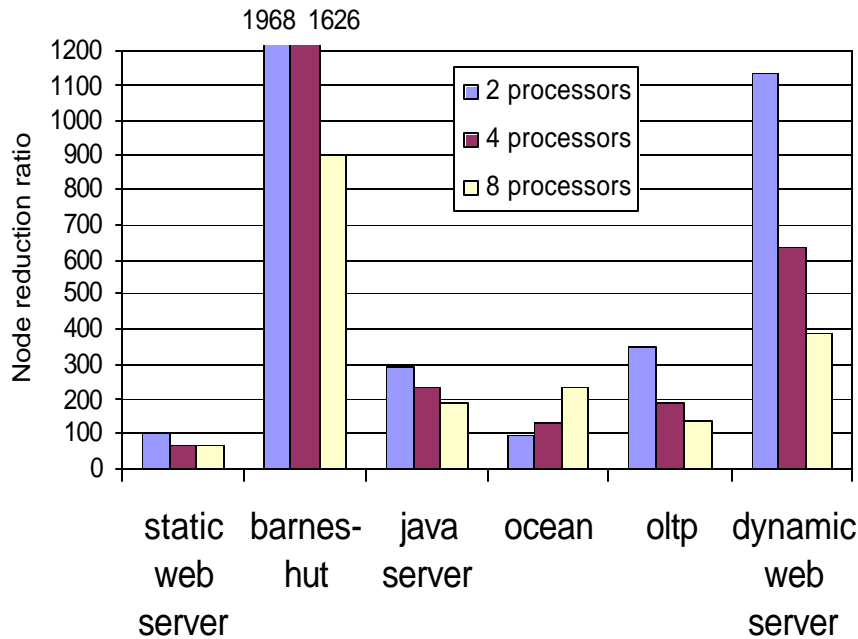
## Java Server



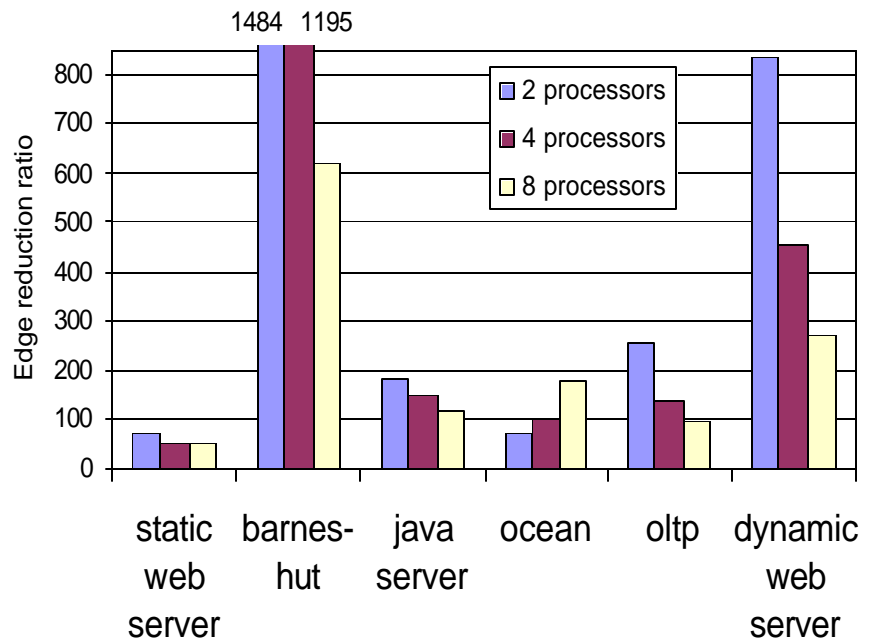
- x-axis: global slack plus one in log scale
- y-axis: fraction of instructions that have global slack = x
- More global slack in directory system
- Directory protocol has higher L2 miss latency because of indirections
- Other workloads have similar results

# Effectiveness of Graph Reduction

Node reduction ratios



Edge reduction ratios



- Reduction ratios range from 66 to 1968
- Average node reduction ratio 485, edge ratio 352
- Maximum node reduction ratio 1968, edge ratio 1484

# Experiments

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- Do instructions really have global slack? How much?
  - Most have global slack  $< 100$  ns, some spikes between 100 and 200 ns
- How critical is an entire processor in a program's execution?
  - A processor's time on critical path closely corresponds with its L2 cache miss rates
- How do different cache coherence protocols affect global slack of instructions?
  - Directory protocol has more global slack
- How effective is graph reduction?
  - Reduction ratios range from 66 to 1968



# Related Work

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- Uniprocessor DAG model and critical path and slack analysis (Fields 2001, 2002)
- Critical path and slack analysis at the procedure level or above for performance bottlenecks (Hollingsworth 1994, 1998, and Yang 1998)
- Multiprocessor scheduling
- DAG reduction (Beckmann 1994, Netzer 1993)

# Conclusions and Future Work

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- We can construct a DAG model for multiprocessor slack
- We can determine criticality by computing global slack in the DAG model
- Experiments show global slack exists and graph reduction effectively reduces DAG size
- Future research will study online algorithms for predicting global slack and design criticality-based processor control policies